

A SURVEY PAPER ON TRAVELLING SALESMAN PROBLEM USING GENETIC ALGORITHM AND BRANCH AND BOUND ALGORITHM

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Abstract:- The Travelling Salesman Problem is very suitable obstacle from NP set. It is still one from NP-hard. The result of TSP has wide range of practical application so; it is required to have one dynamic result for TSP NP-hard problem. A lot of efforts were provided in the prehistory to give time efficient solutions for TSP. Solution should be correct and close. This paper analysis on going the dynamic result to the obstacle uses the Genetic Algorithm to optimize TSP. It is also used for the reducibility of time complexity of TSP.

Keywords: Travelling Salesman Problem, Genetic Algorithm.

I. INTRODUCTION

Traveling Salesman Problem (TSP) may be a classical combinatorial optimization question, which now can only be solved by met heuristics to urge the approximate solution. The traveling salesman problem is sort of simple: a traveling salesman has got to visit customers in several cities, exactly one customer in each city. Since he's curious about not being too long on the road, he wants to require the shortest tour. He knows the space between each two cities which he wants to go to. So far, nobody was ready to come up with an algorithm for solving the travelling salesman problem that doesn't show an exponential growth of run time with a growing number of cities. There's a robust belief that there's no algorithm which will not show this behavior, but no one was ready to prove this (yet). The Pictorial and Mathematical structure of the TSP may be a graph during which the nodes, edges, vertices etc. are termed because the attributes. TSP may be a problem to search out the simplest shortest suitable path by the salesperson to go to n cities in order that we will reach each and each city exactly once & finally involves the initial position with least resources utilization also as time.

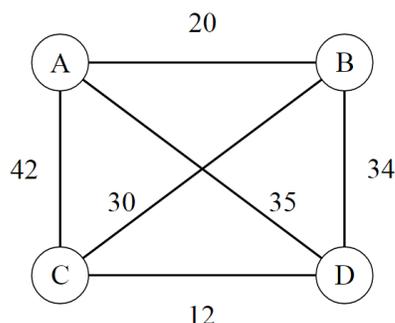


Figure 1 Example of Travelling Salesman Problem

It will be well represented by a graph G having N no. of cities and E no. of paths between cities. Let $G = (N, E)$ be a

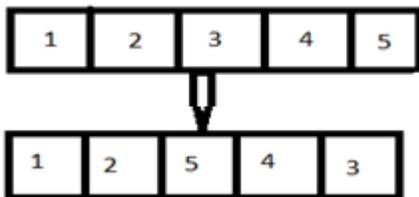
graph where N may be a set of vertices representing cities and E is about of edges representing paths. Let C_{ij} be a price matrix (or distance matrix) related to E. C_{ij} are often defined in Euclidean space as follows: the trail with least values is taken into account as shortest path."The traveling salesmen Problem (TSP) are often commonly defined as:

$$C_{ij} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

Theorem: Cluster n number of cities with known distance among all couple of cities, the major task is to solve an excursion that reaches cities exactly once and also the total distance travelled should be minimized. Formally, TSP can be defined as given an undirected graph and the cost for each edge of that graphs and need to find a Hamiltonian circuit of minimized total cost. It was firstly developed in 1930 as an analytical obstacle and it is ultimate deeply prepared obstacle for advancement.

- A. Solving the TSP: There are many approximate to solve TSP. Many solutions were given to solve TSP since it was developed in 1980. It is effortless to study but tough to explain. It was mainly developed to find the optimal solutions. It is mathematically costly due to it need to examine every explanation so that it finds the most favorable one. Let us consider an example, if we need to travel three cities, but in optimized way. We have $3!$ Ways to visits i.e. 6 ways they find the optimized one. But if we have large number of cities lies 10 cities or 20 cities then factorial of 10 or 20 is very gigantic. So, it is not practically feasible to search the best solution of the problem. We have sorting algorithms for searching the optimized explanation such as K-Nearest Neighbor algorithm and Swarm optimization. These algorithms can give the good enough solution to the TSP. But here we will use Genetic Algorithm as our optimization technique. For finding a solution to TSP we need to require setting up Genetic Algorithm in specialized manner. To use the Genetic Algorithm, it is necessary to used special type of mutation and crossover methods. Initially, mutation method is only able to shuffle the route. It will not even odd or remove a location from the routes, otherwise it will be a risk of creation of a wrong solution. We used the swap mutation method. In this method, two cities are randomly selected and swapped with each other. Now crossover method were be applied to

produce a validate route. In this a subset from the first parent is selected, then add the subset to offspring through these steps.



B. Parents:



C. Offspring:



D. Version of TSP: The Travelling Salesman Problem can be frequently disclosed in two models. The first one is integrative advancement which is the obstacle to find the least Hamiltonian cycle in the plot of different cities. The second one is decision version which is a problem to check the presence of Hamiltonian cycle in a graph smaller than a given density.

Applications: the TSP has several applications even in its purest formulation, such as planning, logistics, and the manufacture of microchips. It appears as a sub-problem in many areas, such as vehicle routing, microchips manufacturing, DNA sequencing, logistics, resource allocation, job sequencing, computer wiring and many more. In these applications, the concept city represents, for example, customers, soldering points, or DNA fragments, and the concept distance represents travelling times or cost, or a similarity measure between DNA fragments. The TSP also appears in astronomy, as astronomers observing many sources will want to minimize the time spent moving the telescope between the sources.

II. LITERATURE REVIEW

S. Lin and B. W. Kernighan presented that this paper focuses to present the integrated overview of few best correct and close algorithms. So far to develop for TSP. Hamiltonian circuit is used to find the path. Few examples given in this paper like computer wiring, wallpaper cutting etc.

G. E. Liepins and M. R. Hilliard presented that in this paper two categories of crossover operations are

considered in association with three penalty function and multi objective advancement. They were hoping to develop broadly applicable, powerful techniques able to handle many problems, Holland was inspired by example of population Genetics and also used crossover instead of mutation.

Gilbert Laporte presented that this paper used searching method for Genetic optimal and immediate optimal solutions for TSP. Here give n by n semantics grid of length among n cities, also find shortest path that reaches all cities only once. This paper uses a different searching technique that finds optimal explanation with large constancy in functioning terms that rises around as n. So this method is time saving and also optimized.

Heinz Muhlenbein presented that in this paper parallel Genetic Algorithms used two main modification as correlated to Genetic Algorithm. Initially, choice for lifetime fitness is assigned. All particulars live in 2-D world. A mate selection done by each particular independently in its neighbored, then, every single particular may advance its fitness mating. The PGA is completely asynchronous.

Chun hua Fu, Lijun Zhang, Xiaojing Wang and Liying Qiao presented that the TSP is a complicated problem. The Vehicle Routing Problem (VRP) and city pipeline optimization can use TSP for solving. It is actual necessary to optimize TSP. but standard Genetic Algorithm has some drawbacks. It is actual famous problem in mathematics also Genetic Algorithm is expanded from the transformation acts of biosphere.

III. PROBLEM FORMULATION

The searching approach of PGA is given by 3 components-

1. Spatial population structure.
2. The crossover operator.
3. The hill climbing strategies.

Problem Space Analysis: As it is quality of travelling salesman problem, the ultimate familiar solutions of the problem were solve to found for make the algorithm unable practicable only for the plot with very small number of knobs. The space analysis of the TSP does not conclude much research over the problem. Travelling Salesman Problem Examples.

	1	2	3	4	5
1	-	10	8	9	7
2	10	-	10	5	6
3	8	10	-	8	9
4	9	5	8	-	6
5	7	6	9	6	-

- A. In this example every node is connected to other node. But the cost is nil to reach the same node from other node. So, there is dash (-).
- B. As they can see every node is connected with every other node. So, various Hamiltonian circuits are possible.
- C. C. they has various solutions like: - 1-2-4-5-3-1, 2-5-1-4-3-2 and so on.
- D. But among all these solutions are need to find the optimal one.

TSP Examples- Formulations

$X_{ij}=1$, If he/she moves immediately i to j .

Aim function is to minimum, the total distance travelled which is given by: $\sum C_{ij}X_{ij}$

where C_{ij} = cost incurred or travelled distance.

For $j=1$ to n , $\sum X_{ij}=1 \forall i$

For $i=1$ to n , $\sum X_{ij}=1 \forall j$

$X_{ij} = 0.01$.

Sub-way Elimination constraints

- They have sub ways of distance n .
- They need to eliminate the length of sub way by making the cost travel from j to i as infinite. $C_{ij}=\infty$.
- For eliminating sub way having length 2, we have $X_{ij} + X_{ji} \leq 1$.
- For eliminating sub way having length 3, we have $X_{ij} + X_{jk} + X_{ki} \leq 2$.
- As there are n nodes, So we can use following constraints:

$nc2$ for length 2

$nc3$ for length 3

$nc(n-1)$ for length $(n-1)$.

TSP Example sub tour

elimination:

	1	2	3	4	5
1	-	10	8	9	7
2	10	-	10	5	6
3	8	10	-	8	9
4	9	5	8	-	6
5	7	6	9	6	-

IV. CONCLUSION

In study various research papers to unravel TSP the algorithms (GA) are proved to be much efficient algorithms than the traditional ones (like dynamic programming, greedy algorithm, branch and bound methods etc.). Heuristic algorithms are simpler for little and mid-sized problems than other algorithms. There are certain issues with these also that are confinement to sub-optimal solution only like stagnation behavior just in case of ACO, premature convergence just Or Add your own word in case of GA and convergence speed in case of PSO. From the start of those approaches tons of amendments are finished improving their performance like different 2 selections, mutation, crossover strategies are given from time to time so as to enhance GA.

Different updating mechanisms and route selection mechanisms and adding memories in ants are implemented for the enhancement in ACO also as in PSO. But still there's tons of labor to try to for betterment of those algorithms. Like their developing are having a vital role in solving different problems supported approximation and forecasting. Those have brought an extra step in evolutionary calculation, by using the crossover, mutation and selection operators those have created a versatile and suitable algorithm for each quite application. The TSP may be a conceptual base of a problem that comes from many real applications. It's on the main target of the many researchers because of its importance, it is widen so much in the aspects of different treatments also in the techniques and methods necessary for its solution. During this work is used GA for locating an approximation for the TSP supported simulations. The GA is relatively good approximate tools even within the TSP.

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